# Stacking behavior of twin-free type-*B* oriented $CeO_2(111)$ films on hexagonal $Pr_2O_3(0001)/Si(111)$ systems

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Tailored  $CeO_2/Pr_2O_3$  thin-film oxide heterostructures are of interest for model catalysis studies by surface science techniques. For this purpose, thin  $CeO_2(111)$  films were grown by molecular beam epitaxy on hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) as well as on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) support systems. A comparative, rigorous structure investigation by reflection high-energy electron diffraction transmission electron microscopy and laboratory and synchrotron based x-ray diffraction is reported. It is found that twin-free, exclusively type-B oriented  $CeO_2(111)$  films are obtained on both oxide supports.  $CeO_2(111)$  films adopt the stacking sequence from the cub-Pr<sub>2</sub>O<sub>3</sub>(111) buffer, but the transfer of the stacking information is less evident in the case of hex-Pr<sub>2</sub>O<sub>3</sub>(0001) films. *Ab initio* calculations are applied to understand the unusual stacking behavior of the  $CeO_2(111)$  on the hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) system. It is revealed that the type-B stacking configuration is the more favorable configuration by 8 eV/nm<sup>2</sup> due to electronic and crystallographic factors.

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## I. INTRODUCTION

Rare-earth oxides (REOs) are of interest in several fields of catalysis, e.g., in oxidative dehydrogenation,<sup>1</sup> oxidative coupling,<sup>2</sup> methane conversion,<sup>3</sup> and three-way catalysis.<sup>4</sup> Especially, the high oxygen mobility and storage capability of REOs, which are the highest for the praseodymium oxide  $Pr_6O_{11}$ ,<sup>5</sup> influence the catalytic activity. The microscopic origin of this behavior arises from the easy exchange in the valence state of  $Pr^{3+}/Pr^{4+}$ , where  $Pr^{3+}$  is the preferred state under many reaction conditions. Interestingly, the neighboring rare-earth element cerium behaves complementary and prefers the Ce<sup>4+</sup> valence state in the oxide form. Combining cerium and praseodymium oxides thus enables us to engineer catalysts with tailored reactivity and selectivity by improving the characteristics of the catalyst, e.g., oxygen storage capacity (OSC), oxygen mobility, and thermal stability.<sup>6-9</sup> If such systems are prepared as single-crystalline thin oxide films on plane substrates, they can be used as model catalyst systems. This approach reduces the complexity of investigating threedimensional (3D) amorphous or polycrystalline materials to surface science studies of two-dimensional (2D) films with specific orientation and defined defect densities. This simplification exhibits the advantage to correlate the catalyst structure with its properties by applying the plethora of surface science tools.<sup>10–12</sup>

For the growth of single-crystalline REO thin films on Si, which might be used as a model catalyst system, a high expertise was developed in the field of microelectronics. Originally, such REOs were investigated for developing high-k dielectrics, <sup>13</sup> setting up engineered Si wafers and integrating

complex functional oxides on Si.<sup>14–20</sup> In the special case of Pr and Ce oxides, different groups already succeeded to grow epitaxial CeO<sub>2</sub> and Pr<sub>2</sub>O<sub>3</sub> thin films on Si(111),<sup>21–25</sup> which could act as appropriate systems for surface science model catalysis. In this paper, we report about combined CeO<sub>2</sub>/Pr<sub>2</sub>O<sub>3</sub> bilayer systems on Si(111), which are of interest as a model catalyst for CeO<sub>2</sub> with enhanced oxygen storage capacity by charging and discharging the buried Pr<sub>2</sub>O<sub>3</sub> layer. Therefore, we have grown CeO<sub>2</sub>(111) on top of cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) supports. Before carrying out model catalytic studies, a rigorous structure study of the CeO<sub>2</sub>/Pr<sub>2</sub>O<sub>3</sub>/Si heterostructure must be elaborated and is reported in this paper.

As a main result, it is found that twin-free, oriented  $CeO_2(111)$  films can exclusively type-B be grown on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) as well as on hex- $Pr_2O_3(0001)/Si(111)$  support systems. The orientation of the BACBAC... stacking sequence of (111) planes in Si is defined as type-A configuration. Fcc-related layers with (111) orientation, the in-plane orientation of which is rotated by 180° with respect to the Si substrate, exhibit a type-B stacking configuration and an ABCABC ... sequence by definition. The growth of type-B  $CeO_2(111)/hexPr_2O_3(0001)/Si(111)$ heterostructures is a surprising result because the stacking information from the Si substrate to the  $CeO_2(111)$  film should get lost due to the ACACAC ... stacking sequence of the hex-Pr<sub>2</sub>O<sub>3</sub>(0001) film. The so-called stacking twin formation (simultaneous presence of type-A and -B domains) is a known heteroepitaxy problem of (111) oriented cubic lattices on hexagonal lattice surfaces, e.g., In<sub>2</sub>O<sub>3</sub>(111)/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>(0001),<sup>26</sup>  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>(111)/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> (0001),<sup>27</sup> and epi-Si(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111).<sup>28,29</sup> The main objective here is to gain an understanding of the stacking formation mechanism by investigating the twin-free, type-B heteroepitaxial growth of CeO<sub>2</sub>(111) on the hex-Pr<sub>2</sub>O<sub>3</sub>(0001) buffer layer in comparison to the case of cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) supports. For this reason, we performed an extensive laboratory and synchrotron based structure analysis in combination with crystallographic considerations and *ab initio* theory studies.

#### **II. EXPERIMENTAL DETAILS**

On-oriented 4" boron-doped Si(111) wafers ( $\rho = 5$ -15  $\Omega$ cm) were cleaned using a standard wet etching process with hydrofluoric acid (HF) and an ammonia fluoride (NH<sub>4</sub>F) buffer, as explained in detail in a previous publication.<sup>30</sup> After this procedure, the hydrogen-terminated Si wafers were loaded into an ultrahigh vacuum chamber (UHV) with a base pressure of  $3 \times 10^{-10}$  mbar. Annealing the samples at 700 °C for 5 min leads to a high-quality  $(7 \times 7)$ -Si(111) surface reconstruction. Oxide granulate, evaporated by an electron beam, was used for the molecular beam epitaxy (MBE). The growth of 8-nm single-crystalline hex-Pr<sub>2</sub>O<sub>3</sub>(0001) film was carried out at 625 °C substrate temperature with a deposition rate of 3 nm/min. For the phase transition to single crystalline, twinfree cub-Pr<sub>2</sub>O<sub>3</sub>(111), an *ex situ* annealing process was used.<sup>31</sup> CeO<sub>2</sub> was grown afterward on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) 22 nm thick and on hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) 38 nm thick at the same temperature and deposition rate. During oxide deposition, the chamber pressure raised typically up to  $1 \times 10^{-6}$  mbar without supply of additional oxygen.

An EK 35 reflection high-energy electron diffraction (RHEED) apparatus (E = 15.8 keV) from Staib Instruments was used for the *in situ* growth control of the oxide film quality and to monitor the stacking information after each deposition step. Cross-section images of the heterostructures along the Si[-110] direction were recorded, using a Philips CM200 transmission electron microscope (TEM) with a point resolution of 0.27 nm. To characterize the global crystal quality in terms of layer orientation, x-ray diffraction (XRD) was carried out ex situ with a DMAX 1500 and a SmartLab from Rigaku [Cu  $K_{\alpha}$  radiation ( $\lambda = 0.154$  nm)]. In addition, synchrotron radiation-grazing incidence x-ray diffraction (SR-GIXRD) measurements at the beam line W1 of the Hamburger Synchrotronstrahlungslabor (HASYLAB) were performed (E = 10.5 keV) to achieve a structure analysis of the CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) heterostructure with high resolution and sensitivity.

Ab initio calculations were carried out with the parallelized pseudopotential plane-wave code QUANTUM ESPRESSO.<sup>32</sup> Exchange and correlation energies were expressed in the local density approximation (LDA) form, as parametrized by Perdew and Zunger.<sup>33</sup> Oxygen, silicon, and hydrogen atoms were described with pseudopotentials from ESPRESSO distribution (ultrasoft pseudopotentials were used for oxygen). For praseodymium and cerium atoms, custom pseudopotentials were treated as semicore electrons.<sup>34</sup> In order to circumvent the LDA problem with the open f shell, the 4f shell was frozen in the core.

Consequently, the lanthanide atoms Ln with valence 3 and 4 ( $Ln^{3+}$  and  $Ln^{4+}$ , where Ln = Ce, Pr) were represented by separate pseudopotentials, meaning that in the calculation they were treated as separate species: the number of felectrons was fixed and no conversion between the Ln<sup>3+</sup> and Ln<sup>4+</sup> "species" was possible during the self-consistent run. All four Ln pseudopotentials included the 5p shell as semicore electrons. The pseudopotentials were verified to be free of ghost states. They reproduced the lattice parameters of the corresponding bulk oxide with an accuracy better than 1%, which is typical for this kind of calculation. Also, the computed bulk moduli were in a satisfactory agreement with the experimental data.<sup>35</sup> For the interface calculations, the Brillouin zone was sampled with eight surface special kpoints equivalent to the  $(\frac{1}{4}, \frac{1}{4}, 0)$  point of the 5 × 3 primitive rectangular surface cell with dimensions  $1.945 \times 2.021 \text{ nm}^2$ , corresponding to volume-relaxed hexagonal Pr<sub>2</sub>O<sub>3</sub> bulk. The energy cutoff for plane waves was set to 40 Ry.

## **III. RESULTS AND DISCUSSION**

## A. RHEED

A RHEED study was applied to *in situ* monitor the structural properties of the CeO<sub>2</sub>/cub-Pr<sub>2</sub>O<sub>3</sub>/Si(111) [Figs. 1(a) and 1(b)] and CeO<sub>2</sub>/hex-Pr<sub>2</sub>O<sub>3</sub>/Si(111) [Figs. 1(c) and 1(d)] heterostructures [electron beam oriented along the stacking sensitive  $\langle -110 \rangle$  azimuth of Si(111)]. The RHEED images [Figs. 1(a)–1(d)] show spotty patterns due to the onset of 3D growth. The latter fact allows deducing first insights regarding the vertical oxide orientation, as described in detail below.

As illustrated by the dashed lines, a twin-free, type-B oriented cub- $Pr_2O_3(111)$  surface diffraction pattern is visible in the RHEED image, Fig. 1(a). This result is in good

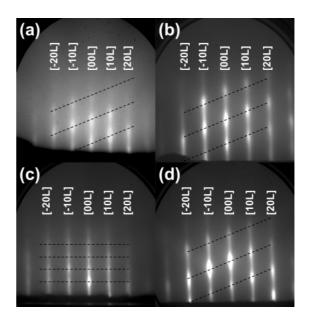


FIG. 1. RHEED images along the Si $\langle -110 \rangle$  azimuth of a (a) type-B oriented cub-Pr<sub>2</sub>O<sub>3</sub>(111) surface on Si(111); (b) type-B oriented CeO<sub>2</sub>(111) surface on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) support; (c) hex-Pr<sub>2</sub>O<sub>3</sub>(0001) surface on Si(111); and (d) type-B oriented CeO<sub>2</sub>(111) surface on hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) support.

agreement with the expected theoretical Bragg peak distribution of cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) systems.<sup>36</sup> After CeO<sub>2</sub> deposition, no substantial change in the intensity distribution of the RHEED pattern is observed. The RHEED image, Fig. 1(b), shows again the typical surface diffraction pattern of a twin-free, type-B oriented CeO<sub>2</sub>(111) film. In consequence, the CeO<sub>2</sub>(111) film adopted the type-B stacking information from the cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) system. This behavior is expected for oxide/oxide epitaxy and was previously reported for similar material systems (e.g., cub-Y<sub>2</sub>O<sub>3</sub>/cub-Pr<sub>2</sub>O<sub>3</sub>).<sup>37</sup> In accord with the RHEED study, the epitaxial relationship of the heterostructure is thus given by CeO<sub>2</sub>(111);  $\langle 1-10 \rangle ||$ cub-Pr<sub>2</sub>O<sub>3</sub>(111);  $\langle -110 \rangle$ .

In Fig. 1(c), the RHEED diffraction pattern of the hex-Pr<sub>2</sub>O<sub>3</sub>(0001) surface is shown. This is in agreement with the expected, theoretical Bragg peak distribution of a (0001) oriented hex-Pr<sub>2</sub>O<sub>3</sub> film.<sup>30</sup> Surprisingly, CeO<sub>2</sub> deposition results in a RHEED image Fig. 1(d), which is identical with Fig. 1(b) and characteristic of a twin-free, exclusively type-B oriented CeO<sub>2</sub>(111) layer. In other words, the RHEED study indicates a CeO<sub>2</sub>(111)(1-10)||hex-Pr<sub>2</sub>O<sub>3</sub>(0001); (11-20)||Si(111);(-110) epitaxial relationship.

In conclusion, one can say that no stacking twins are detectable with RHEED in the  $CeO_2(111)$  film, neither on cub- $Pr_2O_3(111)$  nor on hex- $Pr_2O_3(0001)$ . For a further corroboration of the result, we performed an *ex situ* TEM and XRD structure analysis with better resolution and higher sensitivity.

#### B. TEM

Figures 2(a) and 2(b) show high-resolution transmission electron microscope (HRTEM) cross-section images from CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111), respectively. Along the  $\langle -110 \rangle$  direction, the BACBAC... stacking sequence in the [111] direction of the Si(111) substrate is clearly visible. The stacking

orientation is indicated by an arrow pointing to the [11-1] direction. The approximate positions of the interfaces (IFs) are denoted by arrows at the pictures' sides. As explained in previous studies,<sup>28,37,38</sup> post-deposition oxidation during the phase transition from hexagonal to cubic Pr2O3 results in an IF layer [bright contrast in Fig. 2(a)] between the oxide and the Si(111) substrate. The annealed cub- $Pr_2O_3(111)$ layer exhibits an ABCABC ... stacking sequence, due to a 180° rotation around the [111] surface normal. The indicated [11-1] direction reveals the so-called type-B orientation of the cub-Pr<sub>2</sub>O<sub>3</sub>(111) layer. The (11-1) planes were identified by their  $71^{\circ}$  tilt with respect to the (111) planes. The CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111) IF is difficult to identify due to the similar projected potentials and crystal structures. Thus, its position is identified by IF defects between the oxides. Figure 2(a) highlights the presence of an edge dislocation at the IF, namely, an additional (11-1) plane is present in the smaller CeO<sub>2</sub> lattice with respect to the bigger Pr<sub>2</sub>O<sub>3</sub> lattice. The in-plane lattice mismatch of the  $CeO_2(111)$  and cub- $Pr_2O_3(111)$  planes, which will be discussed in detail later, is partially compensated in this way. The [11-1] directions of the CeO<sub>2</sub>(111) and cub-Pr<sub>2</sub>O<sub>3</sub>(111) layers are parallel to each other, representing the common type-B stacking orientation, which the  $CeO_2(111)$  layer adopted from the cub- $Pr_2O_3(111)/Si(111)$  support.

Figure 2(b) of the CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) heterostructure also reveals an amorphous interfacial layer between the as-grown hex-Pr<sub>2</sub>O<sub>3</sub>(0001) and the Si(111) substrate. This is a surprising result because as-deposited hex-Pr<sub>2</sub>O<sub>3</sub>(0001) films were reported to grow without an IF layer on Si(111) and even the atomic structure for monolayer films was solved by GI-XRD studies.<sup>25,39,40</sup> Therefore, we suggest that, during the deposition of CeO<sub>2</sub>, excess oxygen diffuses to the hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) IF and causes a post-deposition oxidation. In contrast, the CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001) IF is atomically sharp, and no crystal defects were identified in our TEM analysis. Therefore, we expect a smaller in-plane

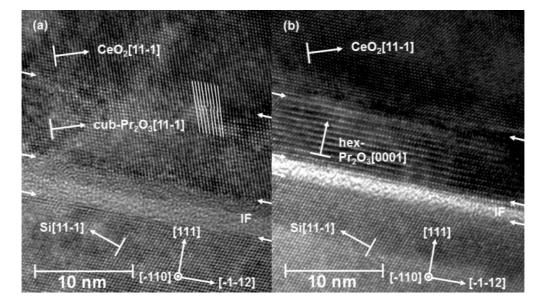


FIG. 2. HRTEM cross-section images along the Si[-110] direction of (a) CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and (b) CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111).

lattice mismatch from the  $CeO_2(111)$  film relative to the hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) support. Furthermore, we can again identify the [11-1] direction of the  $CeO_2(111)$  layer, which is also rotated by 180° with respect to Si[111], confirming with lattice resolution the type-B stacking orientation.

In consequence, RHEED as well as TEM indicates the growth of purely type-B oriented  $CeO_2(111)$  films on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) supports. However, we have to consider that cross-section TEM images only reveal very local and no global information. Therefore, laboratory and synchrotron based XRD studies are applied to complement the structure analysis of the oxide heterostructures on a global scale.

## C. XRD

To explain the direction of the Bragg peaks in the reciprocal space with respect to the Si(111) surface, we have to transform the bulk [hkl] to the surface [HKL] indices and vice versa. Under the assumption that Si and CeO<sub>2</sub> exhibit the same lattice constant, the transformation can be carried out by these operations:

$$\begin{bmatrix} h \\ k \\ l \end{bmatrix}_{\text{bulk}}^{\text{CeO}_2} = \frac{1}{6} \begin{bmatrix} -4 & 4 & 6 \\ -4 & -8 & 6 \\ 8 & 4 & 6 \end{bmatrix} \begin{bmatrix} H \\ K \\ L \end{bmatrix}_{\text{surf}}^{\text{Si}},$$

$$\begin{bmatrix} H \\ K \\ L \end{bmatrix}_{\text{surf}}^{\text{CeO}_2} = \frac{1}{6} \begin{bmatrix} -3 & 0 & 3 \\ 3 & -3 & 0 \\ 2 & 2 & 2 \end{bmatrix} \begin{bmatrix} h \\ k \\ l \end{bmatrix}_{\text{bulk}}^{\text{Si}}.$$
(1)

Accordingly, a schematic drawing of reciprocal space is shown in Fig. 3 for a reciprocal lattice plane spanned by the [111] surface normal and the [11-2] azimuth. To denote the bulk [hkl] and surface [HKL] indices, they are labeled by bulk and surf, respectively. The  $CeO_2$  indices already include the type-B orientation. On top of the sketch, one can see the surface nomenclature to denote the different crystal truncation rods. The Bragg reflections, corresponding to a type-B orientation, are labeled by open circles. Using the  $[10L]_{surf}$  rod as an example, the potential Bragg peaks of type-A oxide twins are also indicated by open squares. Their L positions match to the open circles of the  $[-10L]_{surf}$  rod due to the  $180^{\circ}$  rotation symmetry around the [111] direction of stacking twins. Furthermore, the schematic reciprocal lattice plane discussed in Fig. 3 is identical with the one recorded in our RHEED study (Fig. 1). The dashed lines in Figs. 1(a), 1(b), and 1(d) are reproduced in Fig. 3 and illustrate the common diffraction peak distribution of (111) oriented, fcc-related oxide epilayers.

We start the qualitative XRD structure analysis with wideangle specular  $\Theta$ -2 $\Theta$  scans from 20° to 105° presented in Fig. 4(a). In surface coordinates, this corresponds to a scan along the [00*L*]<sub>surf</sub> rod. These scans allow us to corroborate the vertical epitaxial relationship of the oxide heterostructures on Si(111). The sharp and most intense double peaks can be assigned to  $K_{\alpha 1}$  and  $K_{\alpha 2}$  of the Si(111) reflection and its higher orders (222) and (333). The Bragg peaks of the hex-Pr<sub>2</sub>O<sub>3</sub>(0001) layer [Fig. 4(a), lower curve] are designated as (000*n*) reflections (*n* = 2–6). The (222), (444), and (666) reflections of the cub-Pr<sub>2</sub>O<sub>3</sub>(111) layer [Fig. 4(a), upper curve]

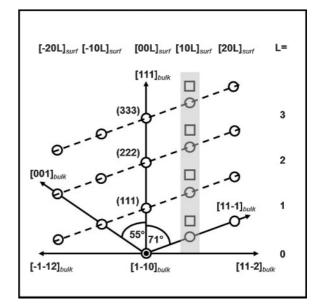


FIG. 3. Schematic drawing of reciprocal space in surface coordinates along the [1-10] direction of fcc-related, (111) oriented surfaces. The open circles are defined to the reflections of a type-B oriented film and in the  $[10L]_{surf}$  rod potential reflections of type-A oriented domains are assigned by open squares.

are also indicated.<sup>25,30</sup> The labeled CeO<sub>2</sub>(111), (222), and (333) reflections are identified to be located close to the positions of the respective Si(*nnn*) (n = 1, 2, 3) Bragg peaks.

In the following, the strain status of the CeO<sub>2</sub> film is analyzed in a quantitative way. Therefore, we first enlarged the section around the Si(222) reflection from  $52.5^{\circ}$  to  $67.5^{\circ}$ [Fig. 4(b)] because the kinematically forbidden Si(222) Bragg peak exhibits the lowest intensity. The CeO<sub>2</sub>(222) reflection at  $2\Theta = 59.24^{\circ}$  (lattice spacing  $d_{(222)} = 1.558$  Å) on the hex- $Pr_2O_3(0001)$  support [Fig. 4(b), lower curve] is close to the theoretical bulk value ( $2\Theta = 59.09^\circ$ ;  $d_{(222)} = 1.562$  Å). In consequence, CeO<sub>2</sub>(111) films grow apparently fully relaxed on hex- $Pr_2O_3(0001)$ . In contrast, the lateral lattice mismatch between  $CeO_2(111)$  and cub- $Pr_2O_3(111)$  should be much bigger so that a strong in-plane tensile strained  $CeO_2(111)$  film is expected, causing compression in vertical direction. Indeed, we observe a shift to higher angles of the  $CeO_2(222)$  reflection  $(2\Theta = 59.84^\circ; d_{(222)} = 1.544 \text{ Å})$  on the cub-Pr<sub>2</sub>O<sub>3</sub>(111) buffer layer [Fig. 4(b), upper curve].

The tetragonal distortion of the oxide lattice can be determined by the so-called  $\cos^2 \chi_{(hkl)}$  method described in Ref. 41, where Bragg reflections of different inclinations  $\chi_{(hkl)}$  are analyzed.  $\chi_{(hkl)}$  is given by the angle between the surface normal of the (111) and the measured (*hkl*) net plane. Under the assumption that the distortion is small compared to the cubic lattice constant *a*, one can calculate from the measured Bragg peak position a theoretical cubic lattice constant  $a_{(hkl)}$ . Thus, plotting  $a_{(hkl)}$  versus  $\cos^2 \chi_{(hkl)}$  allows one to deduce the in-plane lattice constant  $a_0$  at  $\cos^2 \chi_{(hkl)} = 0$ , which is equivalent to a 90° sample tilt. For a direct comparison with the in-plane lattice constant of hex-Pr<sub>2</sub>O<sub>3</sub>, Figs. 4(c) and 4(d) show similar plots with  $a_{(hkl)}/\sqrt{2}$  for CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111), respectively. Therefore, the  $\chi_{(11-1)} =$ 

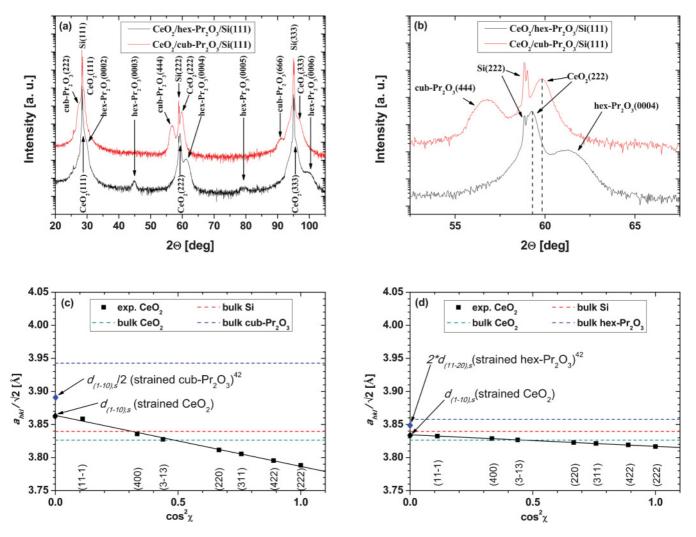


FIG. 4. (Color online) XRD specular  $\Theta$ -2 $\Theta$  measurements of CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) (lower curve) and CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) (upper curve) (a) with a wide angular scan from 20° to 105° and (b) with an enlarged section from 52.5° to 67.5°. Strain measurement using a cos<sup>2</sup>  $\chi$  (*hkl*) plot of the CeO<sub>2</sub>(111) film on (c) cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and (d) hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) support.

 $70.5^{\circ}, \chi_{(400)} = 54.7^{\circ}, \chi_{(3-13)} = 48.5^{\circ}, \chi_{(220)} = 35.3^{\circ}, \chi_{(311)} =$ 29.5°,  $\chi_{(422)} = 19.5^{\circ}$ , and  $\chi_{(222)} = 0^{\circ}$  angles were used for the corresponding reflections. From the linear regression [Fig. 4(c)], a strained in-plane lattice spacing of  $d_{(1-10),s} =$ 3.864 Å can be determined for the  $CeO_2(111)$  film on cub- $Pr_2O_3(111)/Si(111)$ . In comparison to the bulk in-plane lattice spacing  $d_{(1-10),b} = 3.826$  Å, a lateral tensile strain of +0.78% is resulting. In contrast, the tensile strain in the CeO<sub>2</sub>(111) film on hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) amounts to only +0.21% [Fig. 4(d)], resulting from the extrapolated in-plane lattice spacing  $d_{(1-10),s} = 3.834$  Å. The coefficient of determination from the linear regressions amount to  $R^2 =$ 0.992 and  $R^2 = 0.999$  for Figs. 4(c) and 4(d), respectively. We assume that the bigger in-plane tensile strain from  $CeO_2(111)$ on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) compared to CeO<sub>2</sub>(111) on hex- $Pr_2O_3(0001)/Si(111)$  is caused by the bigger lattice mismatch. Therefore, we have previously to consider the strained in-plane lattice spacings of hex-Pr<sub>2</sub>O<sub>3</sub>(0001) ( $2d_{(11-20),s} = 3.849$  Å) and cub-Pr<sub>2</sub>O<sub>3</sub>(111)  $(d_{(1-10),s}/2 = 3.890 \text{ Å})$  on Si(111), which were determined to be typical results in a thickness range from 4–13 nm.<sup>42</sup> These values are indicated in Figs. 4(c) and 4(d). Note that cub-Pr<sub>2</sub>O<sub>3</sub>(111) has a four times bigger in-plane surface unit cell than Si(111). From these results, a lattice mismatch of bulk CeO<sub>2</sub>(111) ( $d_{(1-10),b} = 3.826$  Å) to strained hex-Pr<sub>2</sub>O<sub>3</sub>(0001) buffer layers (-0.60%) and to cub-Pr<sub>2</sub>O<sub>3</sub> buffer layers (-1.65%) arises. As expected, the cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) support exhibits the bigger lattice mismatch, causing the bigger strain in the CeO<sub>2</sub>(111) film.

To analyze now the stacking characteristics, we need in-plane as well as off-plane information. Figures 5(a) and 5(b) show  $\Phi$  scans around the Si[111] axis of the CeO<sub>2</sub>{-111} and Si{-111} reflections from CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) (2 $\Theta$  = 28.4°) and CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) (2 $\Theta$  = 28.5°) heterostructures. Due to the high crystal quality of the silicon wafers, the sharp peaks can be easily assigned to the Si{-111} reflections. These are separated by 120° around the [111] surface normal, due to the threefold off-plane symmetry around the cubic Si(111) space diagonal (*Fd*-3*m*). Accordingly, the broader CeO<sub>2</sub>{-111} peaks are rotated by 180° in respect to the Si{-111} peaks in Figs. 5(a) and 5(b). This experimental result is a clear proof of the type-B orientation of the CeO<sub>2</sub>(111) film,

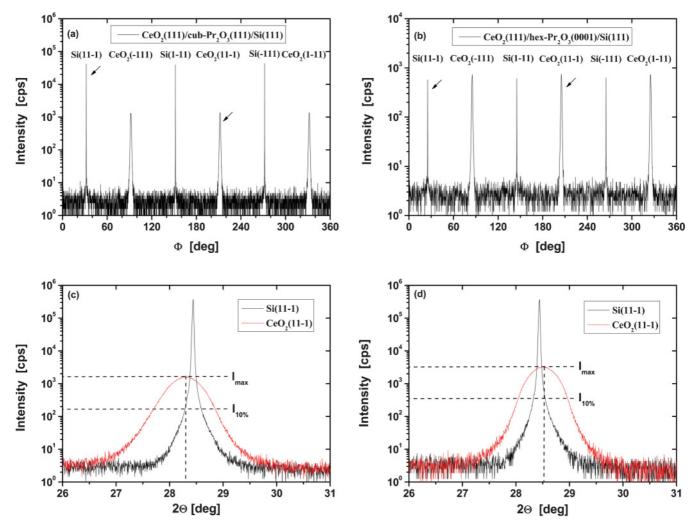


FIG. 5. (Color online) Twin analysis via  $\Phi$  scan around the Si[111] axis (a) at  $2\Theta = 28.4^{\circ}$  of CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) (b) at  $2\Theta = 28.5^{\circ}$  of CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111). HRXRD  $\Theta$ -2 $\Theta$  scans on the Si(11-1) Bragg peak (the broad peak) and the CeO<sub>2</sub>(11-1) Bragg peak (the sharp peak) with  $\Phi$  rotated about 180° of (c) CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) and (d) CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111).

which confirms the CeO<sub>2</sub> $\langle 1-10 \rangle ||cub-Pr_2O_3\langle 1-10 \rangle ||Si\langle -110 \rangle$  and CeO<sub>2</sub> $\langle 1-10 \rangle ||hex-Pr_2O_3\langle 11-20 \rangle ||Si\langle -110 \rangle$  lateral epitaxial relationships.

The absence of stacking twins or rather type-A domains had to be verified by HRXRD measurements. Therefore, the Si(11-1) and CeO<sub>2</sub>(11-1) reflections [labeled by arrows in Figs. 5(a) and 5(b)] are compared to each other in Fig. 5(c) [CeO<sub>2</sub>(111)/cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111)] and Fig. 5(d)  $[CeO_2(111)/hex-Pr_2O_3(0001)/Si(111)]$  by  $\Theta$ -2 $\Theta$  scans. The respective Si(11-1) (sharp peak) and  $CeO_2(11-1)$  (broad peak) reflections are related to each other by a 180° in-plane rotation. Referring to the maximum intensity  $I_{max}$  of the CeO<sub>2</sub>(11-1) peak, we conclude that no type-A CeO<sub>2</sub> Bragg peak is present at the position of the Si(11-1) peak with an intensity of more than 1/10 of the type-B CeO<sub>2</sub> Bragg peak intensity  $[I_{10\%}]$ criteria in Figs. 4(c) and 4(d)]. In other words, as no shoulder is visible in the Si(11-1) Bragg peak on the position of the  $CeO_2(11-1)$  reflection, we can estimate from the HRXRD study that less than 10% of the CeO<sub>2</sub> film might exhibit a type-A stacking on the cub- $Pr_2O_3(111)/Si(111)$  as well as on the hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) support. To give a more precise estimate of the type-A/B ratio in the  $CeO_2(111)$  film on the hex- $Pr_2O_3(0001)$  buffer layer, high-sensitivity SR-GIXRD studies are discussed in the following.

#### D. SR-GIXRD

For CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) heterostructures, we performed SR-GIXRD scans along the  $[10L]_{surf}$  rod [Fig. 6(a)] and  $[01L]_{surf}$  rod [Fig. 6(b)]. Aside from Si(111) surface coordinates, important Bragg peaks are labeled in bulk coordinates. Concerning the  $[10L]_{surf}$  rod [Fig. 6(a)], the (11-1) and (220) peak positions of the type-A Si(111) are located at L = 1/3 and 4/3 r.l.u., respectively. Due to the 180° in-plane rotation of the type-B oriented CeO<sub>2</sub>(111) film, its (002) and (113) reflections are located at L = 0.670 and 1.675 r.l.u., respectively. However, the potential XRD signals of a type-A stacking CeO<sub>2</sub> domain would overlap again with the peak positions of the more intense type-A Si substrate. In addition, it is noted that the Pr<sub>2</sub>O<sub>3</sub> reflections (10-1*n*) along the  $[10L]_{surf}$  rod appear at L = 0.517n r.l.u. (n = 1, 2, 3,...)

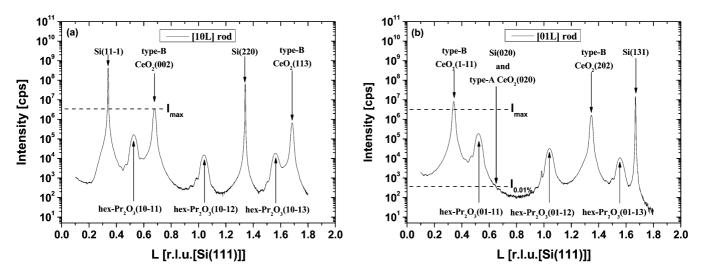


FIG. 6. SR-GIXRD of CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) along the (a) [10L]<sub>surf</sub> rod and (b) [01L]<sub>surf</sub> rod.

because the (0001) lattice spacing of hex- $Pr_2O_3$  is about twice as big as the Si(111) net plane distance.

To achieve a more precise stacking twin analysis, the  $[01L]_{surf}$  rod is studied [Fig. 6(b)]. Again, the hex-Pr<sub>2</sub>O<sub>3</sub> reflections (01-1*n*) are located at L = 0.517n r.l.u. (n = 1, 2, 3,...). On the  $[01L]_{surf}$  rod, we can identify the CeO<sub>2</sub>(1-11) and (202) reflections at L = 0.335 and 1.340 r.l.u. of type-B  $CeO_2(111)$  film. Here, the type-A Si(131) peak is visible at 5/3 r.l.u. and the kinematically forbidden Si(020) reflection is located at L = 2/3 r.l.u. As the latter reflection is forbidden, this exhibits the chance to detect the potential presence of type-A stacking CeO<sub>2</sub> domains with high precision at this position. The fact that also the allowed  $CeO_2(020)$  reflection is not visible with 0.01% intensity  $I_{0.01\%}$  of the CeO<sub>2</sub>(002) maximum intensity  $I_{max}$  corroborates finally the previous discussions that no type-A oriented  $CeO_2(111)$  domains can be found in the type-B oriented  $CeO_2(111)$  layer on the hex- $Pr_2O_3(0001)/Si(111)$  support within the detection limit, even with such a potent investigation method as SR-GIXRD.

#### E. Ab initio calculations

Next, we discuss the physical mechanisms responsible for the observed growth of twin-free, type-B oriented  $CeO_2(111)$ on hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111). As outlined in the Introduction, it is by far not self-evident that the type-B interface is strongly preferred. In order to elucidate the reasons for this preference, we performed ab initio calculations for interfaces of type-B [Fig. 7(a)] and type-A [Fig. 7(b)]. The results are in agreement with the experimental data and reveal that the interface of type-B is strongly favored, with the energy difference amounting to 2.2 eV per surface cell, i.e., to 8  $eV/nm^2$ . In brief, we find that this effect is attributed to an interplay of electronic and crystallographic factors. First, the valence mismatch at the  $CeO_2/Pr_2O_3$  interface layer leads to conversion of  $Pr^{3+}$  to  $Pr^{4+}$ , i.e., to the reduction of the number of f electrons on Pr from two to one. Second, the interface of type-B corresponds to a topologically smooth transition from  $CeO_2$  to  $Pr_2O_3$ , while the interface of type-A leads to the appearance of a topological stacking fault. The details are explained below.

For completeness, the interface between the oxides and the interface to Si were included in the calculation. For the latter, the configuration determined by Jeutter *et al.*<sup>40</sup> was used. This interface contains an additional layer of oxygen bonded to Si needed to compensate the bonding-type mismatch between Pr<sub>2</sub>O<sub>3</sub> and Si and to bind all electrons donated by  $Pr^{3+}$ . Similar mismatch appears at the interface between CeO<sub>2</sub> and hex-Pr<sub>2</sub>O<sub>3</sub>, where it is compensated by electrons from Pr. The interfacial Pr atoms lose one f electron each and transform from  $Pr^{3+}$  (light blue) to  $Pr^{4+}$  (dark blue). This produces a monatomic PrO<sub>2</sub> interface layer and conserves the semiconducting character of the CeO<sub>2</sub>/Pr<sub>2</sub>O<sub>3</sub> interface. As a result, all Ln atoms (Ce<sup>4+</sup>, Pr<sup>4+</sup>) at the chemical interface have the same valence and prefer the same arrangement of oxygen neighbors, namely, that of cubic LnO<sub>2</sub>, the fluorite structure.

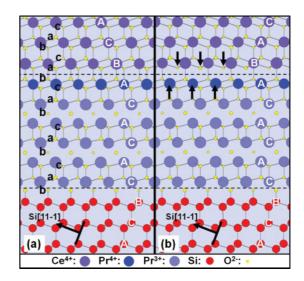


FIG. 7. (Color online) Stacking configuration models along the Si[-110] direction of (a) type-B CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) and (b) type-A CeO<sub>2</sub>(111)/hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111).

The interface of type-B [Fig. 7(a)] provides this arrangement in a natural way, resulting from the stacking of atomic planes in both materials. This becomes apparent by looking at the sublattice of the hex-Pr<sub>2</sub>O<sub>3</sub> layer. Indeed, the praseodymium sublattice exhibits the ACACAC... stacking sequence, while the stacking of the oxygen sublattice follows the bacbac... pattern, as pointed out by Eyring and his notation.<sup>43</sup> After the conversion to PrO<sub>2</sub> at the interface, the Pr<sub>2</sub>O<sub>3</sub> film becomes a topological continuation of the CeO<sub>2</sub> film above it. Since the oxygen sublattice of CeO<sub>2</sub> exhibits the same bacbac... stacking sequence as in Pr<sub>2</sub>O<sub>3</sub>, the only structural adjustment that takes place at the interface is some relatively minor shift of interfacial oxygen atoms of the praseodymium oxide. These atoms move toward the bulk Pr2O3 in response to the increased positive charge of interfacial Pr atoms. The C-terminated geometry, in which all Pr<sup>4+</sup> atoms of layer A in Fig. 7 are substituted by Ce<sup>4+</sup> atoms, is likely to be energetically comparable to the A-terminated geometry assumed in Fig. 7. Namely, this substitution conserves the charge of metal atoms, and also the distance between B and A layers in  $CeO_2$  is close to the distance between the B and A layers at the chemical interface, as well as to the distance between the interfacial A layer and the C next layer in  $Pr_2O_3$ . This topological coherence between hex- $Pr_2O_3(111)$ and  $CeO_2(111)$  provides also a natural means to compensate any local thickness variations on the monatomic scale.

In other words, when the interface is of type-A [Fig. 7(b)], there is a topological (111) stacking fault between  $PrO_2$  and  $CeO_2$ . The interface oxygen atoms of the  $CeO_2$  film are out of registry for the  $Pr^{4+}$ , causing a reduced coordination for the  $Pr^{4+}$  and for the interfacial oxygen atoms [indicated in Fig. 7(b) by arrows]. We, thus, conclude that the observation of twin-free, exclusively type-B growth of  $CeO_2(111)/hex-Pr_2O_3(0001)/Si(111)$  heterostructures is attributed to the formation of a  $PrO_2$  interface layer in response to valence mismatch between a lanthanide dioxide and a lanthanide sesquioxide, to similar stacking of oxygen atomic planes in hexagonal sesquioxide and in the cubic dioxide, and to purely geometrical differences in the stacking of atomic planes for interfaces of types A and B.

#### IV. CONCLUSION AND OUTLOOK

In summary, we have grown epitaxial  $CeO_2/cub-Pr_2O_3/Si(111)$  and  $CeO_2/hex-Pr_2O_3/Si(111)$  heterostructures with MBE monitored by RHEED, which showed the following vertical and azimuthal epitaxial relationships for the respective heterostructures:

$$\begin{split} & \text{CeO}_2(111); \langle 1\text{-}10\rangle \| \text{cub-Pr}_2\text{O}_3(111); \langle 1\text{-}10\rangle \| \text{Si}(111); \langle -110\rangle, \\ & \text{CeO}_2(111) \langle 1\text{-}10\rangle \| \text{hex-Pr}_2\text{O}_3(0001); \langle 11\text{-}20\rangle \| \text{Si}(111); \langle -110\rangle. \end{split}$$

However, this result is very surprising because, on the ACA-CAC... stacking sequence of the hex- $Pr_2O_3(0001)/Si(111)$ support, the stacking information for an ABCABC ... pattern of  $CeO_2(111)$  planes should be lost. So we had to corroborate the RHEED results with further measurements. HRTEM confirmed the epitaxial relationships with atomic resolution. Additionally, an edge dislocation was highlighted in the  $CeO_2(111)$  film on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111), which is based upon in-plane lattice mismatch and the corresponding lateral tensile strain. The strain status could be verified by XRD, approximating the in-plane lattice spacings in a  $\cos^2 \chi_{(hkl)}$  plot for  $CeO_2(111)$  on cub-Pr<sub>2</sub>O<sub>3</sub>(111)/Si(111) (+0.78%) and on hex- $Pr_2O_3(0001)/Si(111)$  (+0.21%). The vertical and lateral epitaxial relationships were confirmed on a global scale by  $\Theta$ -2 $\Theta$  and  $\Phi$  scans, respectively. The amount of type-A domains in the type-B  $CeO_2(111)$  layer was determined to be much less than 10% by laboratory HRXRD measurements. An SR-GIXRD study of the  $[10L]_{surf}$  rod and the  $[01L]_{surf}$ rod finally revealed that even less than 0.01% type-A CeO<sub>2</sub> domains can be detected in the  $CeO_2(111)$  film on the hex-Pr<sub>2</sub>O<sub>3</sub>(0001)/Si(111) support.

Theoretical *ab initio* calculations demonstrated that this type-B stacking configuration of  $CeO_2(111)$  net planes is caused by geometrical differences. First, an interfacial  $PrO_2$  layer is formed to conserve the semiconducting characteristics. Due to this dioxide formation, the type-B interface provides a topological continuation of the bacbac... stacking sequence of the oxygen sublattice. In contrast, a type-A interface would form a (111) stacking fault, reducing the coordination of the interfacial praseodymium and oxygen atoms. Thus, the type-B stacking configuration is preferred by 2.2 eV per surface cell, i.e., by 8 eV/nm<sup>2</sup>, in comparison to the type-A interface.

In view of future model catalytic application, experiments concerning the charging and discharging of the  $Pr_2O_3$  buffer layer with oxygen will be performed. Furthermore, the deposition of mixed  $Ce_{1-x}Pr_xO_{2-\delta}(x = 0 - 1)$  exhibits the opportunity to tune the OSC as well as the oxygen mobility. Adsorption of different gases and the resulting influence to electrical characteristics in dependence of the stoichiometry will be of interest.

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